

NAME: \_\_\_\_\_

BEM 103 QUIZ 5

1. Please define the efficient portfolio frontier:\_\_\_\_\_The set of portfolio with minimal variance condition on return\_\_\_\_\_

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2. Stock A has expected return  $r_A$  and stock B has return  $r_b$  What is the expected return of a portfolio is weighted  $W_A$  on stock a and the rest  $W_B$  on Stock B? \_\_\_\_\_

Let  $r_p$  be the portfolio return. \_\_\_\_\_ $r_p = W_A r_A + W_B r_b$  \_\_\_\_\_

3. Stock A has variance  $\sigma_A^2$ , stock B has variance  $\sigma_B^2$ , and the two stocks have covariance  $\sigma_{AB}$  if a portfolio is equally weighted with each stock what is its variance? \_\_\_\_\_

Let  $\sigma_p^2$  be the portfolio variance.  $\sigma_p^2 = W_A^2 \sigma_A^2 + 2W_A W_b \sigma_{AB} + W_B^2 \sigma_B^2$

In the case of the equally weighted portfolio  $\sigma_p^2 = 0.25\sigma_A^2 + 0.5\sigma_{AB} + 0.25\sigma_B^2$

4. Suppose  $r_A > r_b$ . What portfolio produces a return equal to  $r^*$  where  $r_A > r^* > r_B$ ? what is its variance? \_\_\_\_\_We need to find  $W^*$  such that \_\_\_\_\_ $r^* = W^* r_A + (1 - W^*) r_b$

$$r^* = W^* r_A + (1 - W^*) r_B \Leftrightarrow r^* = W^* (r_A - r_B) + r_B$$

$$\text{Or } W^* = (r^* - r_B) / (r_A - r_B)$$

$$\sigma_p^2 = \left( \frac{r^* - r_B}{r_A - r_B} \right)^2 \sigma_A^2 + 2 \left( \frac{r^* - r_B}{r_A - r_B} \right) \left[ 1 - \left( \frac{r^* - r_B}{r_A - r_B} \right) \right] \sigma_{AB} + \left[ 1 - \left( \frac{r^* - r_B}{r_A - r_B} \right) \right]^2 \sigma_B^2.$$